UNREASONABLE EFFECTIVENESS OF NOISE

TRAINING VIA HYPERPARAMETERS PATH OPTIMIZATION

Mykola Maksymenko, R&D Director, **SoftServe**

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WITH

VLAD PUSHKARIOV, TECHNION
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MACIEJ KOCH-JANUSZ, ETH ZURICH

- TRAINING IN A JOINT WEIGHTS-HYPERPARAMETER SPACE
- EFFICIENT SAMPLING OF THE HYPERPARAMETERS
- NON-STATIONARY SCHEDULING PROTOCOL
- FASTER AND BETTER TRAINED MODELS

GOAL: OPTIMAL, SIMPLER, UNIVERSAL
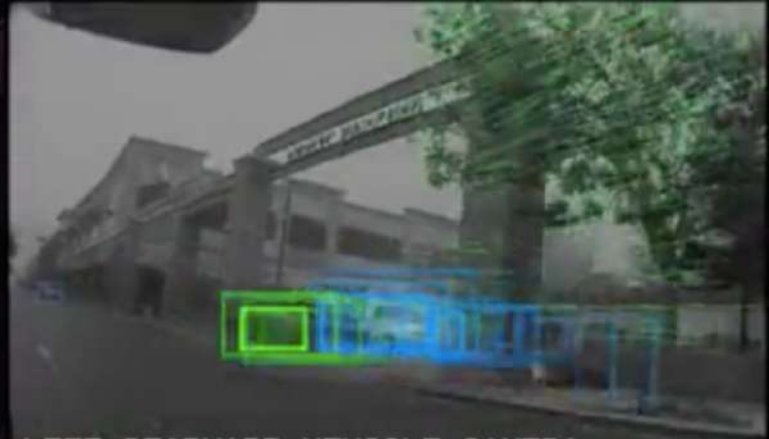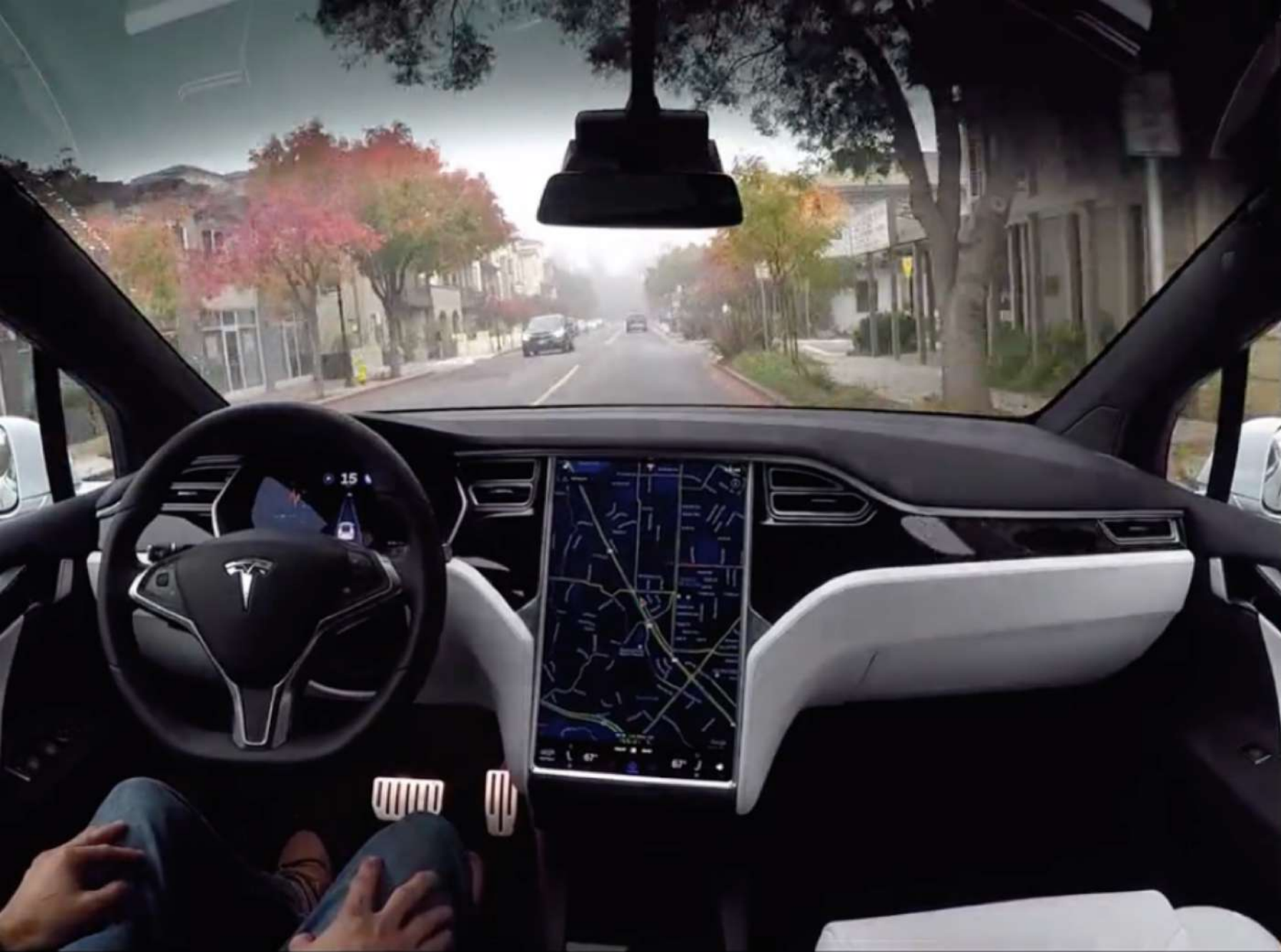
PHYSICS → MACHINE LEARNING

Formalism (energy, noise, etc)
Toy **models**
Concepts and **Ideas** (e.g. spin glass, tensor networks)
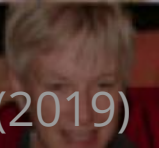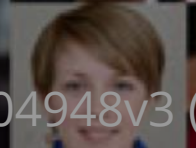etc...

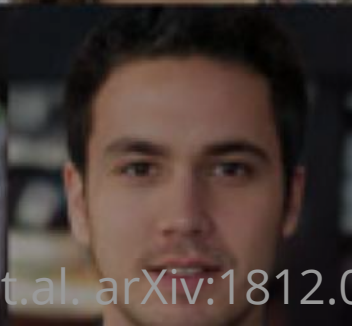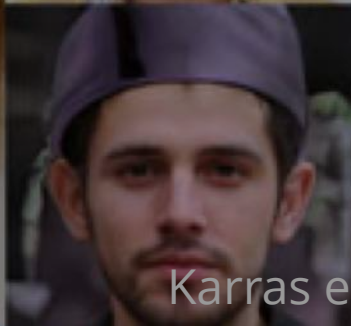softserve

LEFT REARWARD VEHICLE CAMERA

MEDIUM RANGE VEHICLE CAMERA

RIGHT REARWARD VEHICLE CAMERA

MOTION FLOW   LANE LINES   LANE LINES   ROAD FLOW   IN-PATH OBJECTS   ROAD LIGHTS   OBJECTS   ROAD SIGNS

MECHANICS OF NEURAL NETWORKS

$$a_j^{(1)} = \sigma\left(\sum_i w_{ij}^{(1)} x_i + b_j^{(1)}\right)$$

x_1

x_2

x_n

$$a_j^{(f)} = \sigma\left(\sum_i w_{ij}^{(f)} a_i^{(1)} + b_j^{(f)}\right)$$
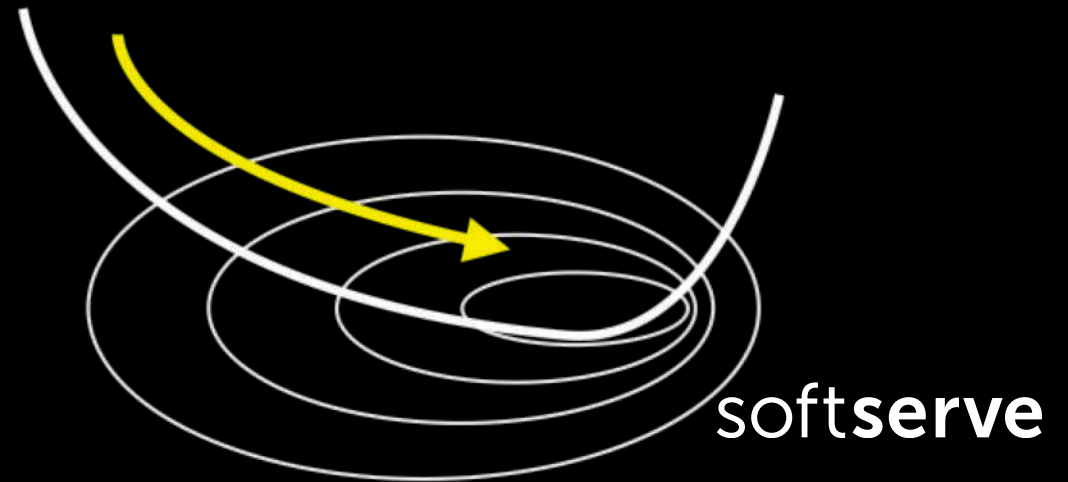
$$\text{Cost} = \frac{1}{2n} \sum_x \|a^f(x) - y_{\text{true}}(x)\|^2$$
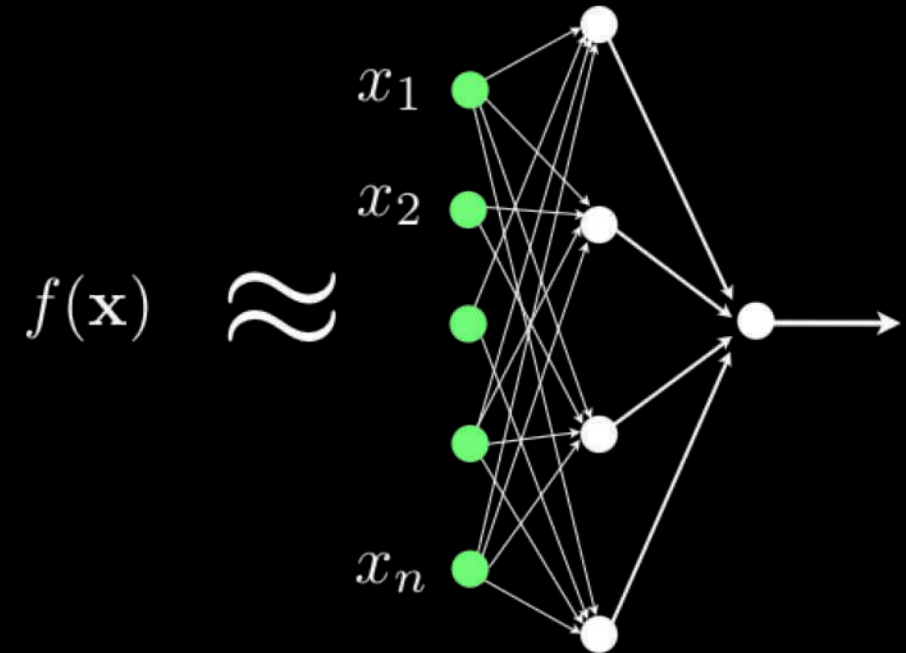
$$w_{ij_{t+1}} = w_{ij_t} - \gamma \nabla_{w_{ij}} Cost$$

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SHOULD WORK WELL IN THEORY...

Kolmogorov-Arnold representation theorem (1956-1963)

Universal approximation theorem, Cybenko (1989)

$$f(x_1, \ldots x_n) =$$

$$\sum_{j=1}^{2n+1} g_j \left(\sum_{i=1}^{n} \phi_{ij}(x_i) \right)$$

$$f(\mathbf{x}) \approx$$

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40+ YEARS TO ADOPT IN PRACTICE

DEEP ARCHITECTURE + BAG OF TRICKS

DEEP ARCHITECTURE
+ BAG OF TRICKS

BATCH GRADIENT
DROUPOUT
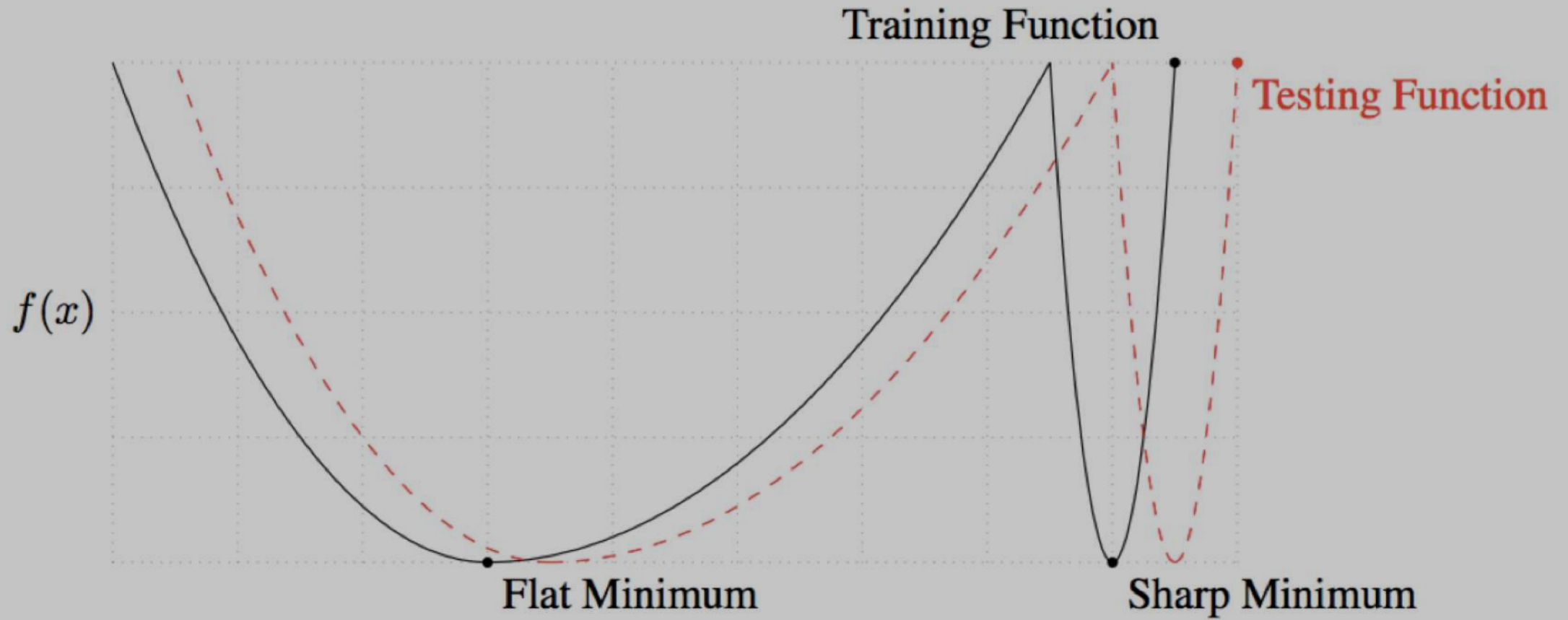EARLY STOPPING
ETC...

DEEP ARCHITECTURE
+ BAG OF ~~TRICKS~~ NOISE
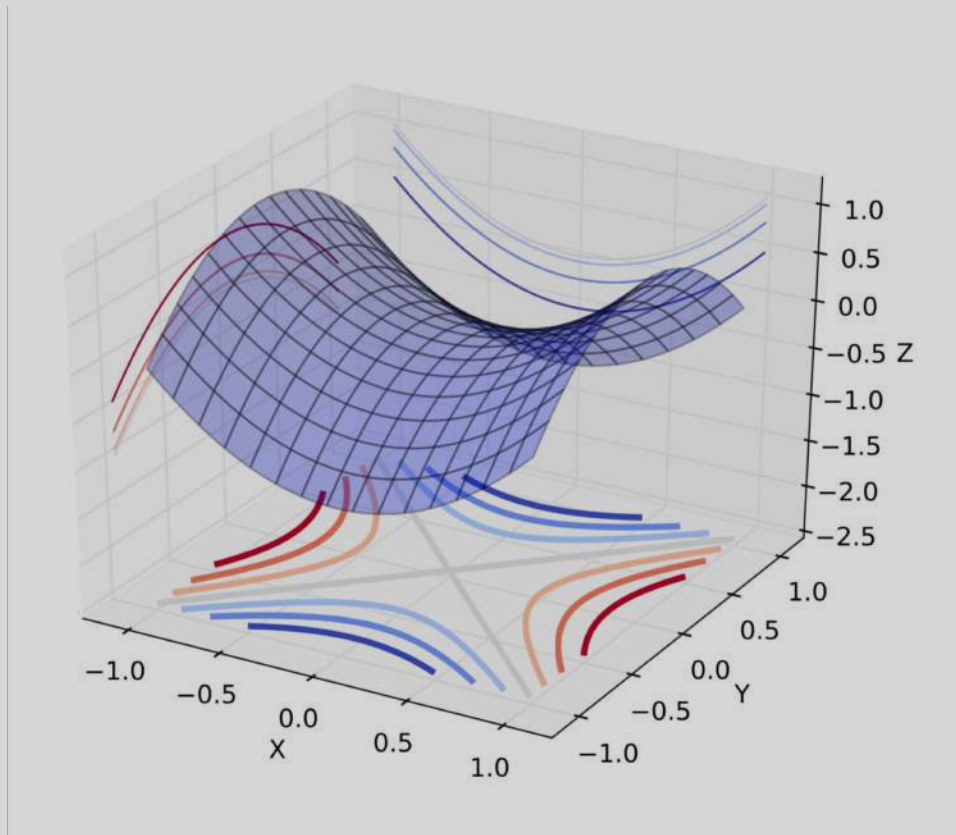
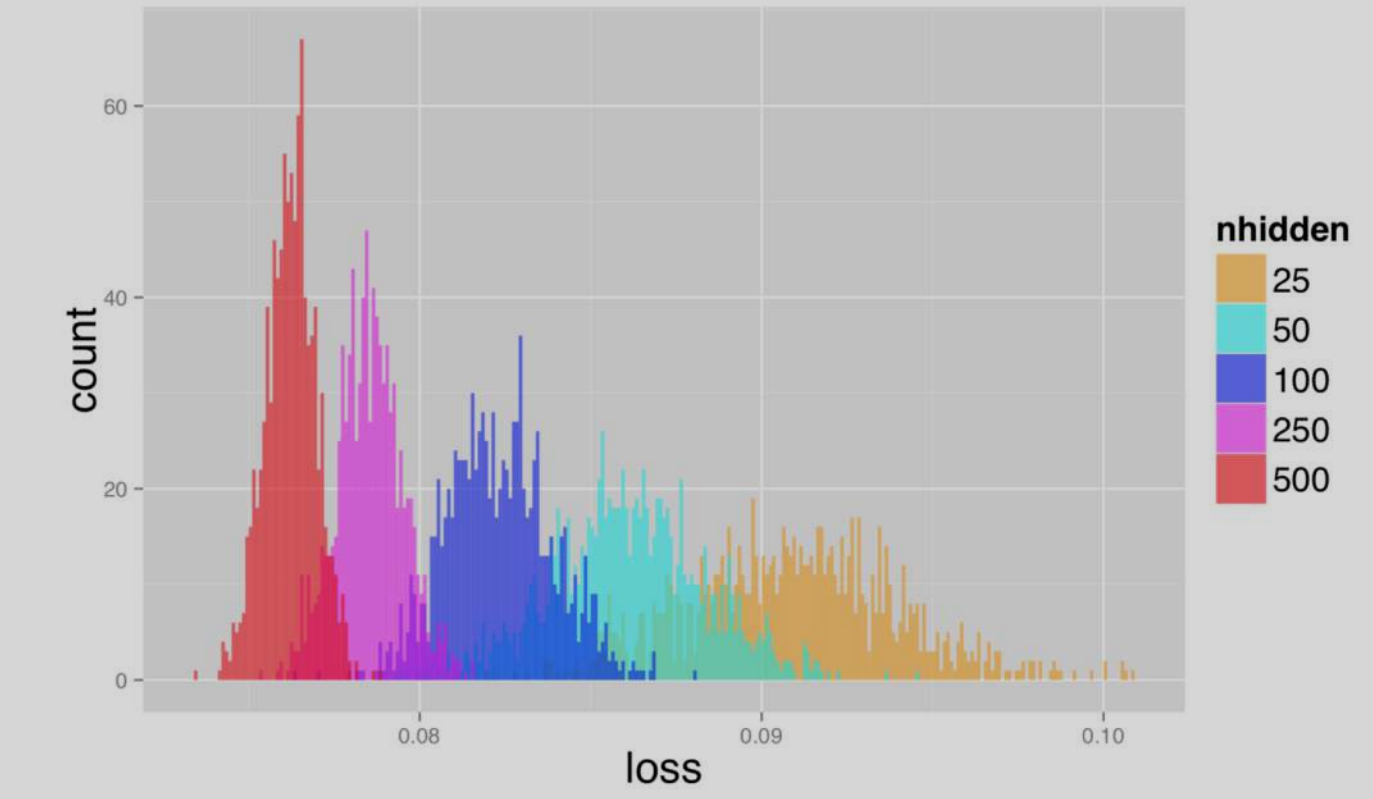# BATCH GRADIENT
DROUPOUT
EARLY STOPPING
ETC...

COMMON WISDOM: BATCH NOISE HELPS TO AVOID "BAD" MINIMA

Training Function

Testing Function

$f(x)$

Flat Minimum

Sharp Minimum

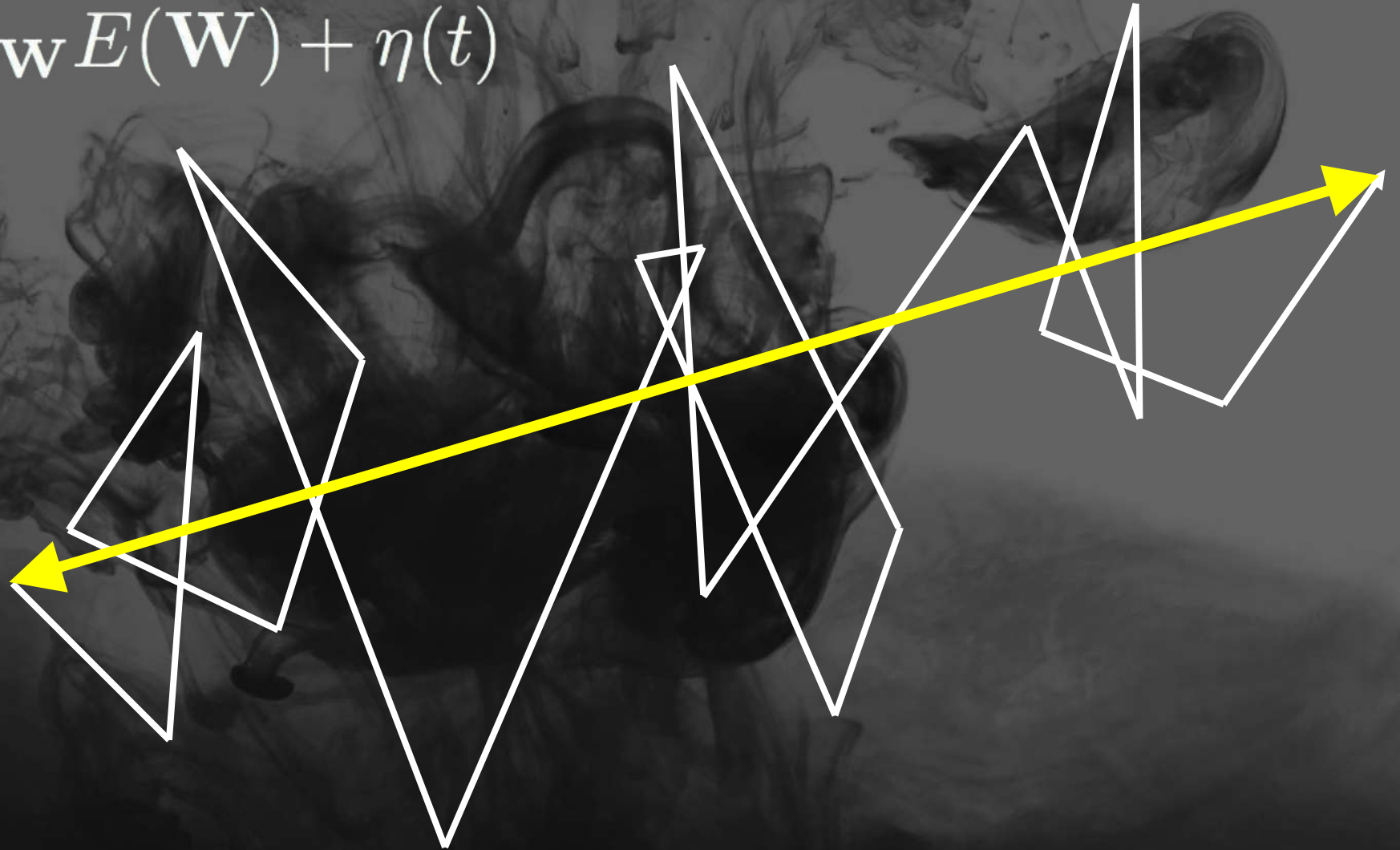# HOW LIKELY ARE THE "BAD" MINIMA?

arXiv:1406.2572v1 (2014)

arXiv:1412.0233v3 (2015)

VERY UNLIKELY!

NOISE SPEEDS UP THE DIFFUSION!

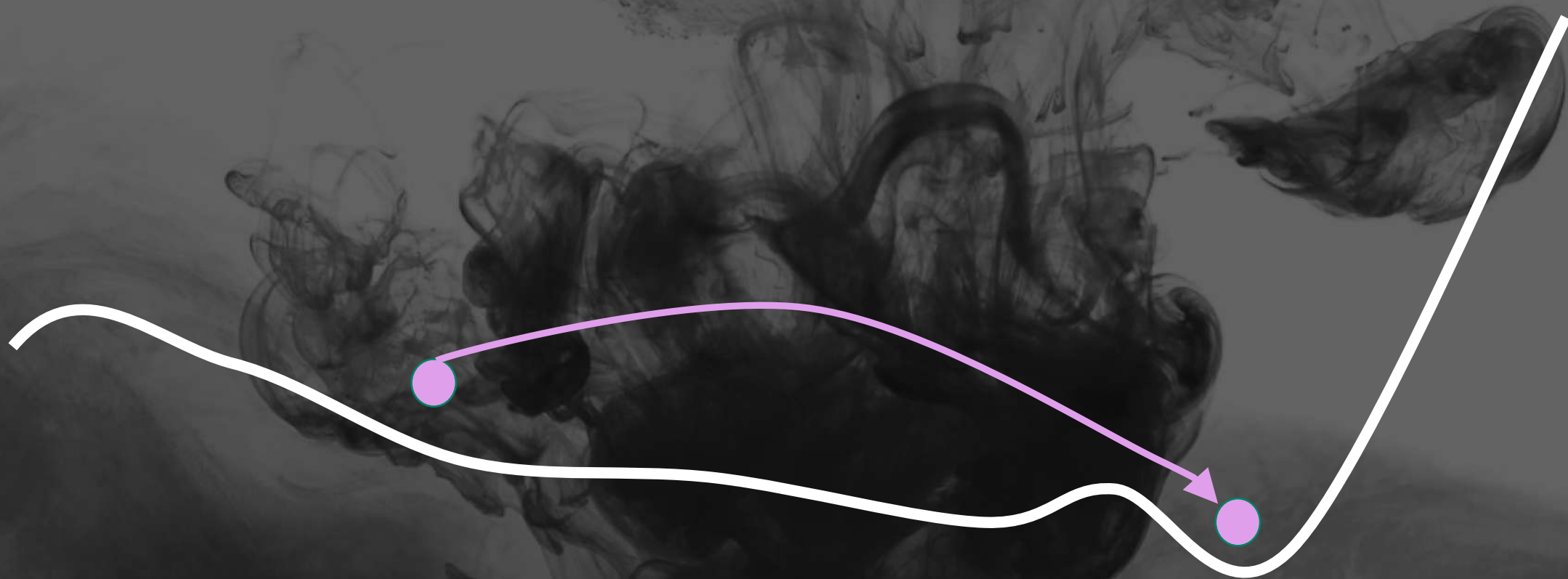$$\frac{\partial \mathbf{W}}{\partial t} = -\nabla_{\mathbf{W}} E(\mathbf{W}) + \eta(t)$$
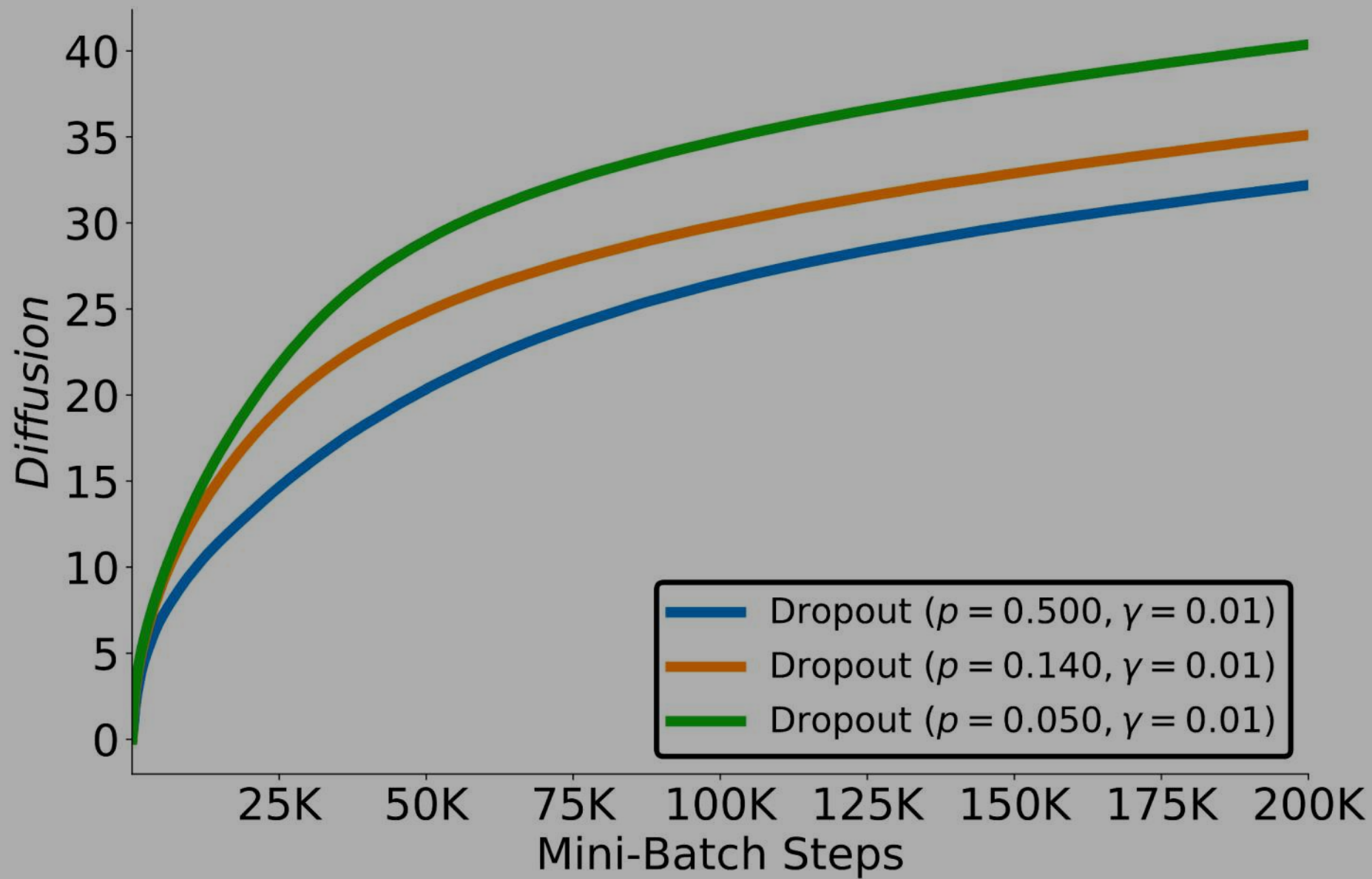
NOISE SPEEDS UP THE DIFFUSION!
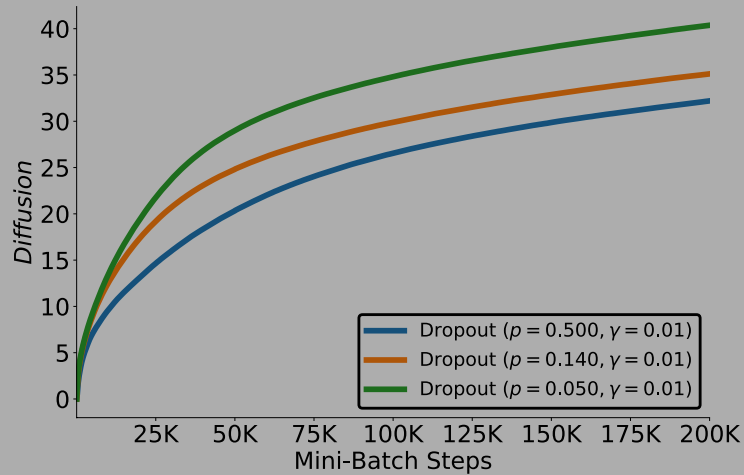
NOISE SPEEDS UP THE DIFFUSION!

JOINT WEIGHT-HYPERPARAMS SPACE

GREEDY APPROACH – POPULATION BASED TRAINING

Jaderberg, et.al. arXiv:1711.09846

JOINT WEIGHT-HYPERPARAMS SPACE

GREEDY APPROACH – POPULATION BASED TRAINING

GAN population development

FuN population development

4.2   4.5   4.8   5.1   5.4   5.7   6.0   6.3   6.6
Inception Score

1000 2000 3000 4000 5000 6000 7000 8000 9000
Cumulative Expected Reward

Jaderberg, et.al. arXiv:1711.09846

JOINT WEIGHT-HYPERPARAMS SPACE

GREEDY APPROACH – POPULATION BASED TRAINING

Jaderberg, et.al. arXiv:1711.09846

EXPLOITING NOISE-LIKE PROPERTY

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OPTIMIZATION OVER THE PATH

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Algorithm 1 Training with replica exchange

INPUT: Number of replicas M, Inverse "temperature" (hyperparameters) $\beta = (\beta_1, \beta_2, \ldots, \beta_M)$
Number of steps for initialization ΔN_i
Number of SGD steps between exchanges ΔN_e
Exchange normalization parameter C
Number of steps T

OUTPUT: Weight configurations $\mathbf{W} = (\mathbf{W_1}, \mathbf{W_2}, \ldots, \mathbf{W_M})$ of the replicas,
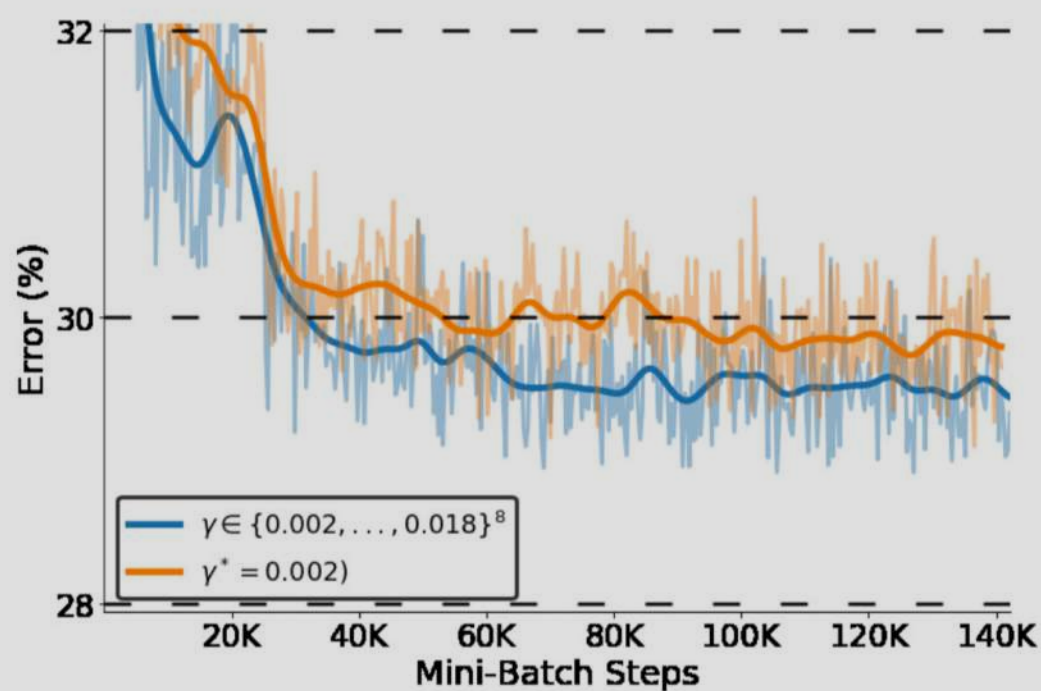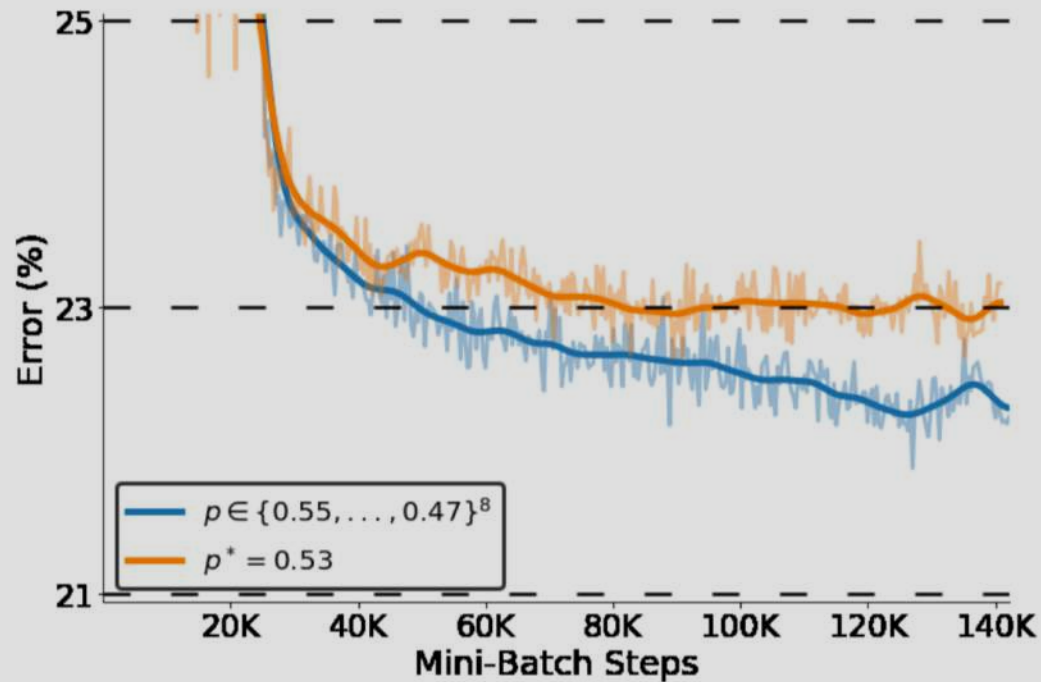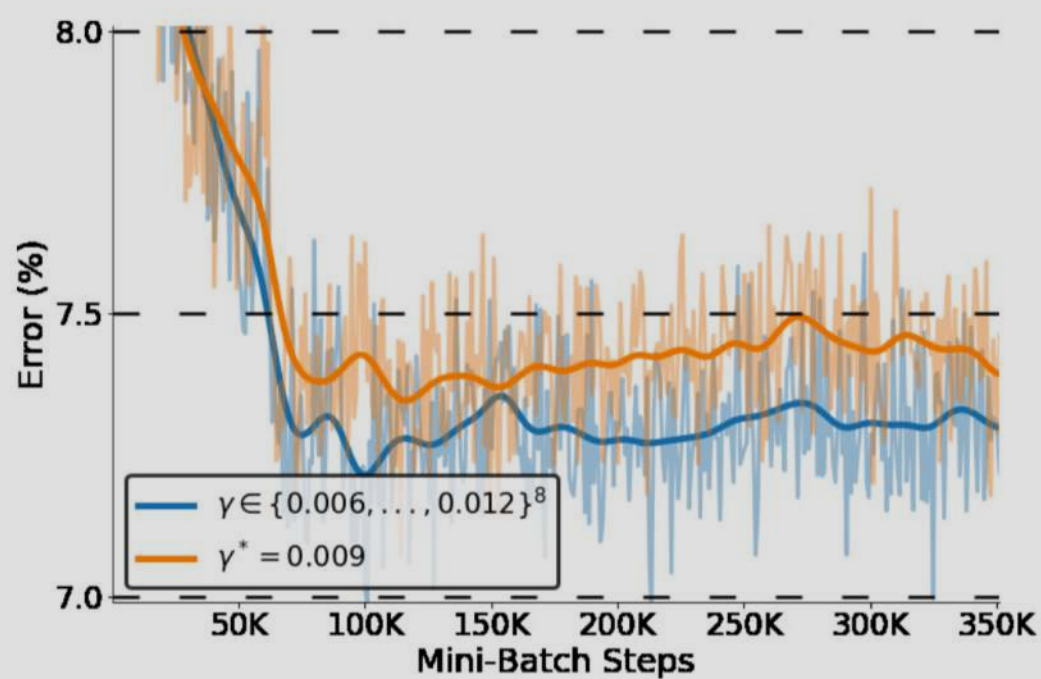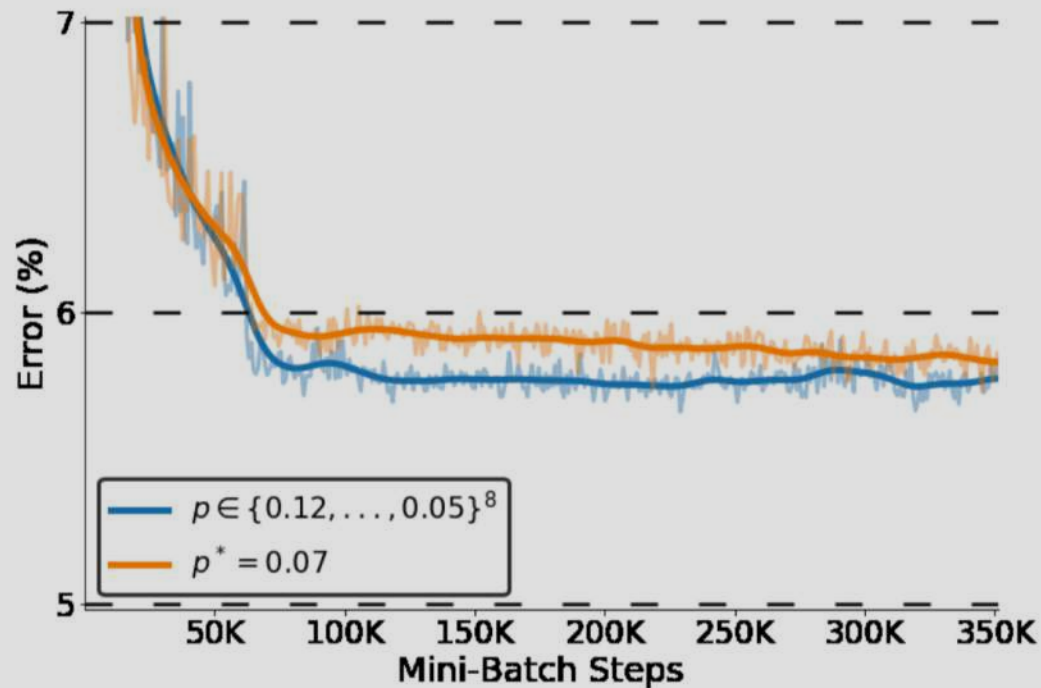 1: **Initialization:** $\forall k \in M$, initialize weights $\mathbf{W}_k$ for each replica and set $t = 0$.
  2: $\forall k \in M$, perform SGD for ΔN_i steps. Update $t \leftarrow t + 1$ at each step.
  3: **Repeat:**
  4:      $\forall k \in M$, perform SGD for ΔN_e steps to update $\mathbf{W}_k$. Set $t \leftarrow t + 1$ at each step.
  5:      Let $\mathcal{L}_t = (\mathcal{L}(\mathbf{W}_1^t), \mathcal{L}(\mathbf{W}_2^t), \ldots, \mathcal{L}(\mathbf{W}_k^t))$ be validation losses at time t.
  6:      Randomly select a pair (m, n) of replicas with adjacent temperatures.
  7:      **if** $\Delta = C(\beta_m - \beta_n)[\mathcal{L}(\mathbf{W}_m) - \mathcal{L}(\mathbf{W}_n)] \leq 0$ **then**
  8:          swap β_m and β_n
  9:      **else**
 10:          swap β_m and β_n with probability $\exp(-\Delta)$.
 11:      Update α, the acceptance ratio. Finish if $t > T$.

EMNIST

Error (%)

25 — 23 — 21

$p \in \{0.55, \ldots, 0.47\}^8$
$p^* = 0.53$

20K 40K 60K 80K 100K 120K 140K
Mini-Batch Steps

Error (%)

32 — 30 — 28

$\gamma \in \{0.002, \ldots, 0.018\}^8$
$\gamma^* = 0.002)$

20K 40K 60K 80K 100K 120K 140K
Mini-Batch Steps

CIFAR10

Error (%)

7 — 6 — 5

$p \in \{0.12, \ldots, 0.05\}^8$
$p^* = 0.07$

50K 100K 150K 200K 250K 300K 350K
Mini-Batch Steps

Error (%)

8.0 — 7.5 — 7.0

$\gamma \in \{0.006, \ldots, 0.012\}^8$
$\gamma^* = 0.009$

50K 100K 150K 200K 250K 300K 350K
Mini-Batch Steps

RESNET/CIFAR10

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THANKS FOR ATTENTION

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